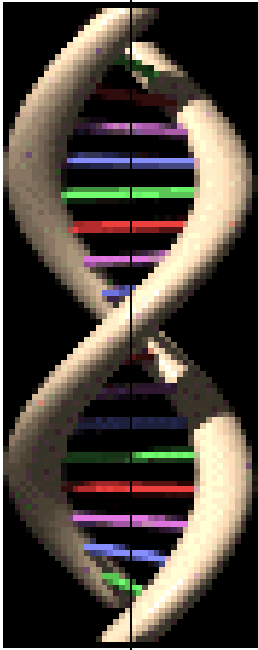


# Electrostatic Interactions in Mixtures of Cationic and Anionic Biomolecules: Bulk Structures and Induced Surface Pattern Formation

*Monica Olvera de la Cruz*

*F. J. Solis, P. Gonzalez-Mozuleos (theory)  
E. Raspaud, J.L. Sikorav,  
M.J. Bedzyk, Y. H. Cheng,  
J. Libera (Experiments)  
Y. Velichko (Simulations)*



## Double Stranded DNA

2 chains each with -1 charge every base pair 3.4 Å

Diameter 20 Å

Persistence length (rigidity) of 500 Å (150 basepairs)

Hydrophilic (hides hydrophobic units)

Projection of the two phosphates on the double-helix axis gives  
**linear charge density :**

**Double Stranded DNA:**  $1 e / 1.7 \text{ \AA} \sim 6 e / \text{nm}$

(short=rod; long=semi-flexible)

**Single Stranded DNA:**  $1 e / 3.4 \text{ \AA}$

(flexible)

DNA is one of the most highly charged systems.

**Strong polyelectrolyte**

Synthetic example: Poly-Styrene-Sulphonate (100% S):  $1 e / 2.5 \text{ \AA} \sim 4 e / \text{nm}$ .

Persistence length 10 Å

# Strong Polyelectrolyte Solutions Physical Properties

**Water soluble in monovalent salts at low ionic strength solutions.**

**Simple model:**

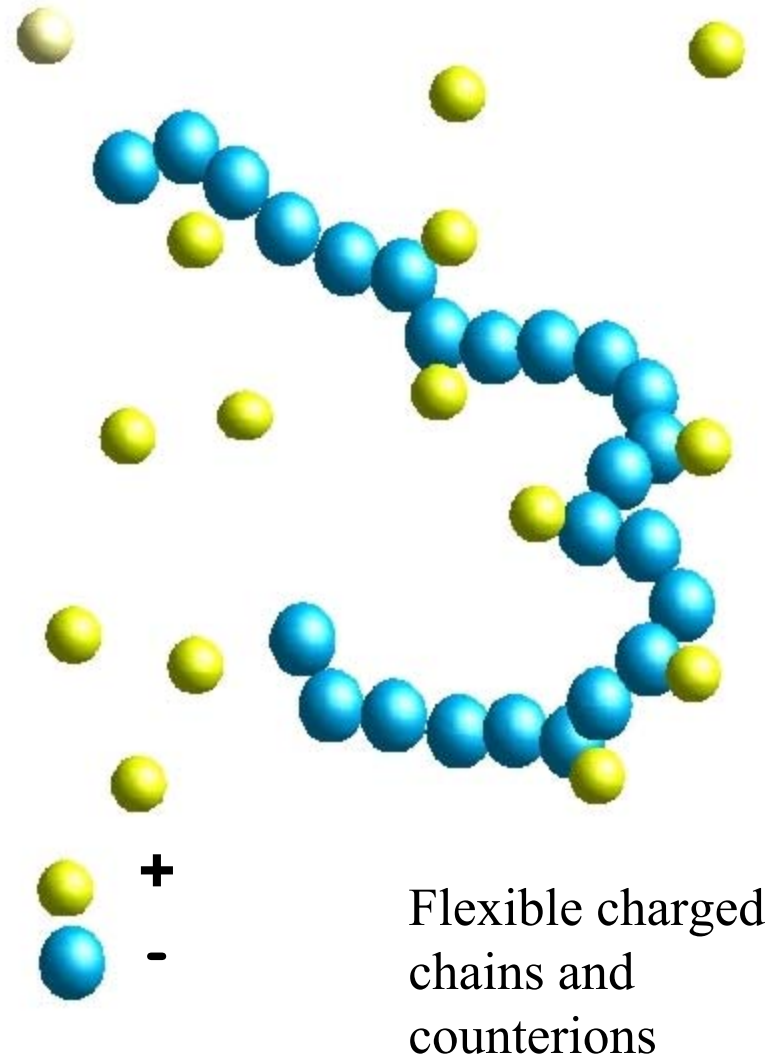
**charged chain (flexible, semiflexible or rod-like)**

**Solvated charge groups and ions**

**Water is structureless**

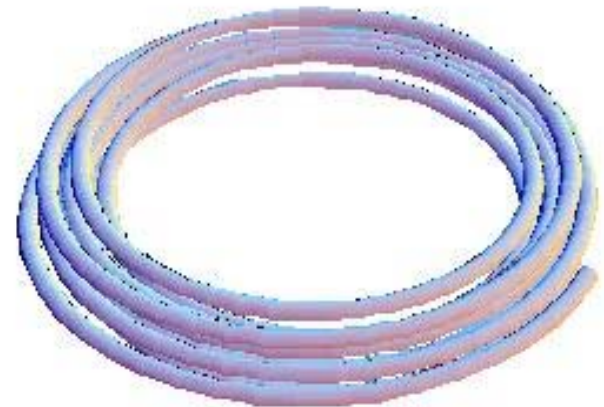
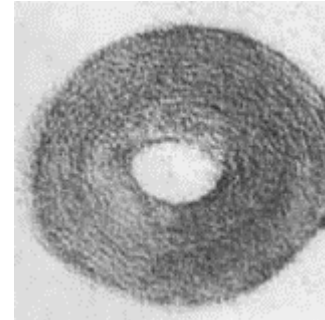
**Chains are stretched to decrease electrostatic repulsions**

.

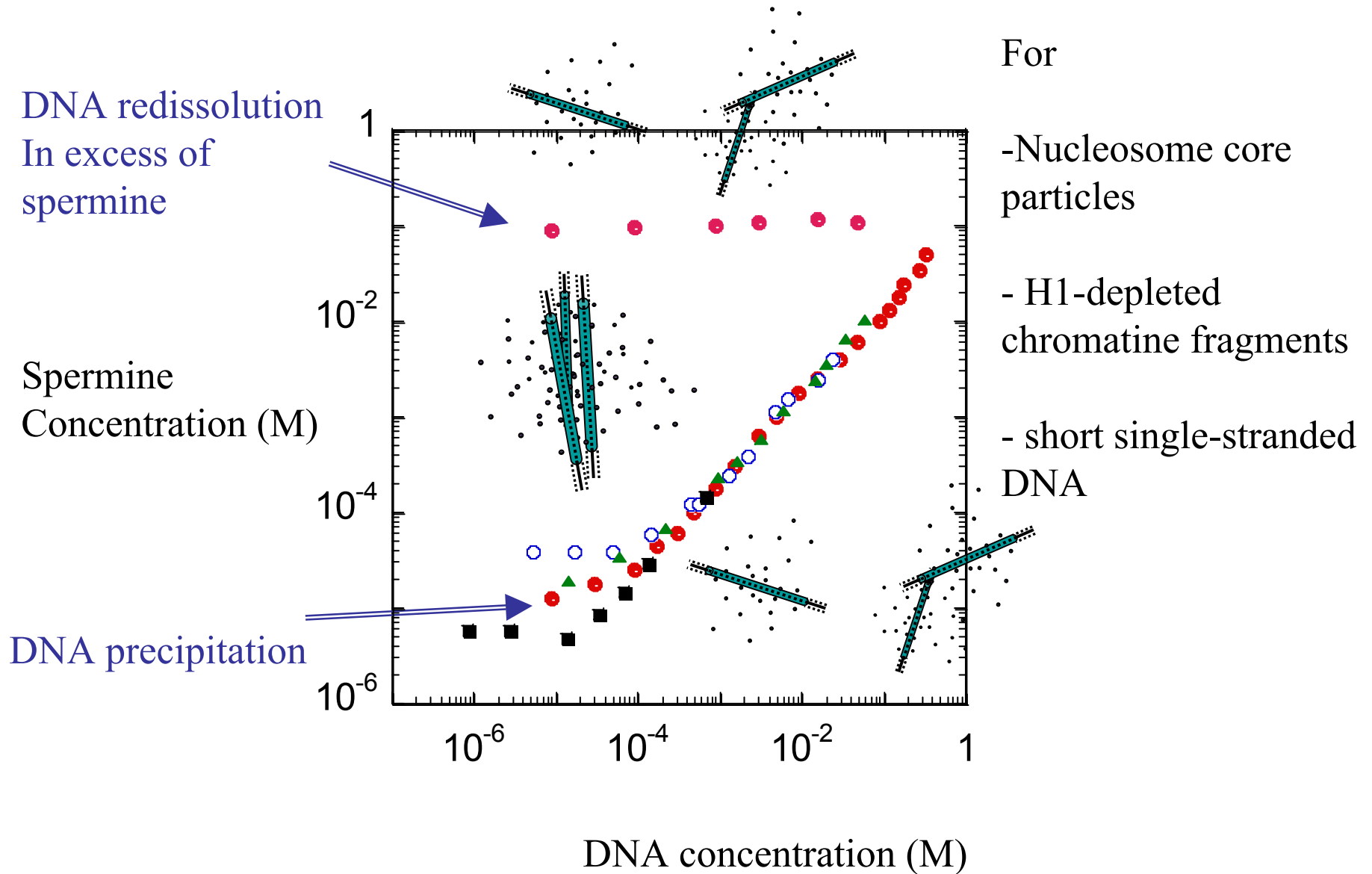


# DNA Condensation: precipitation occurs upon the addition of multivalent salt

- Metallic or organic 3+, 4+, higher multivalent salts (Cobalt hexamine, Spermine, Spermidine) precipitate DNA into toroidal bundles.
- Single stranded DNA and other flexible polyelectrolytes form compact structures.
- J. Widom and R.L. Baldwin, *J. Mol. Biol.*, 144 (1980).
- 



# Phase diagram: nearly universal



(Raspud et al., 1998-99)

# Precipitation/condensation of polyelectrolytes

- Why do equal charges attract?
- The origin of the counterion driven attraction.
- Necessary elements to construct a theory.

# Electrostatically driven self-assembly

- **Cationic-Anionic Biological Complexes**

**Viral assembly**

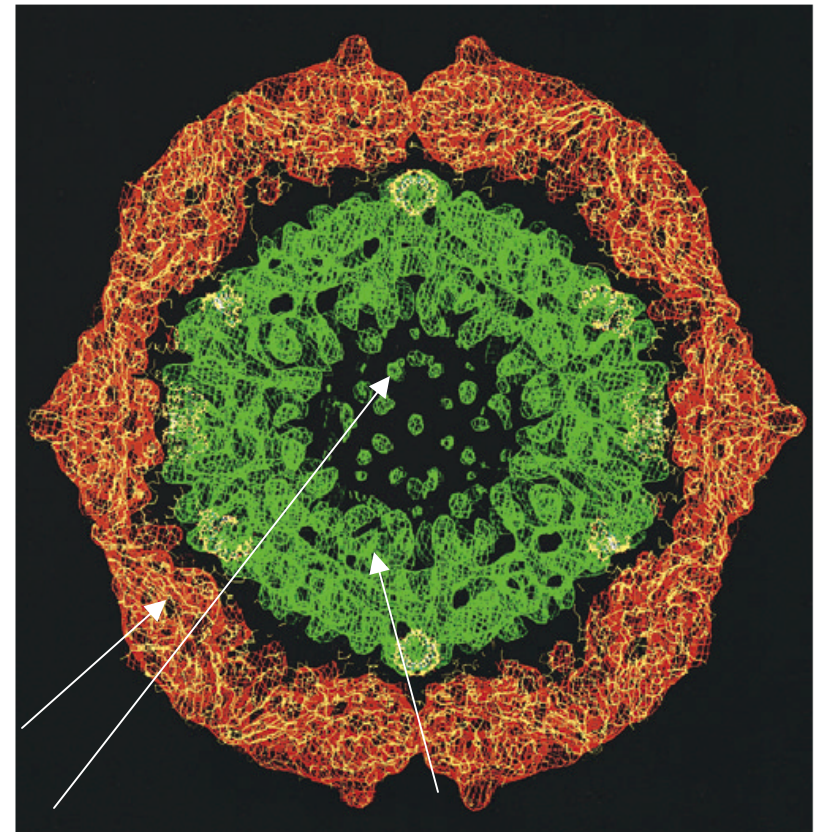
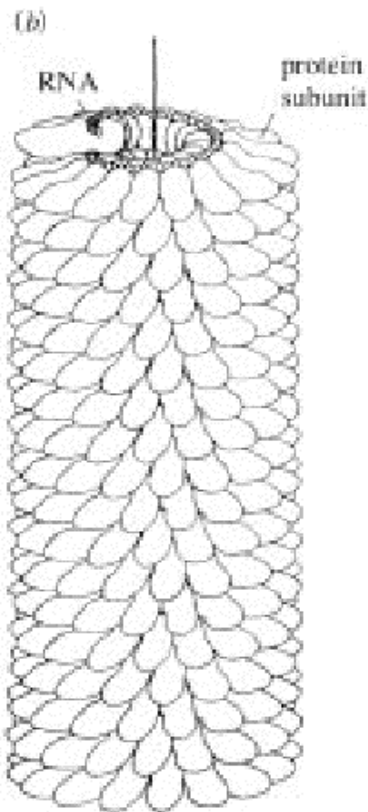
**Chromosomes structure**

**DNA packing for gene therapy**

**Biotechnology (DNA condensation is used to increase DNA denaturation and cyclization rates by orders of magnitude as in vivo)**

# Virial Assembly: Helical and Sphere-like RNA Virus (Tsuruta et al.)

Tobacco Mosaic Virus. One RNA (-)  
molecule of 6,300 base + 2,000  
identical capsid (+) proteins



Self-assembles from capsid protein + viral RNA solution

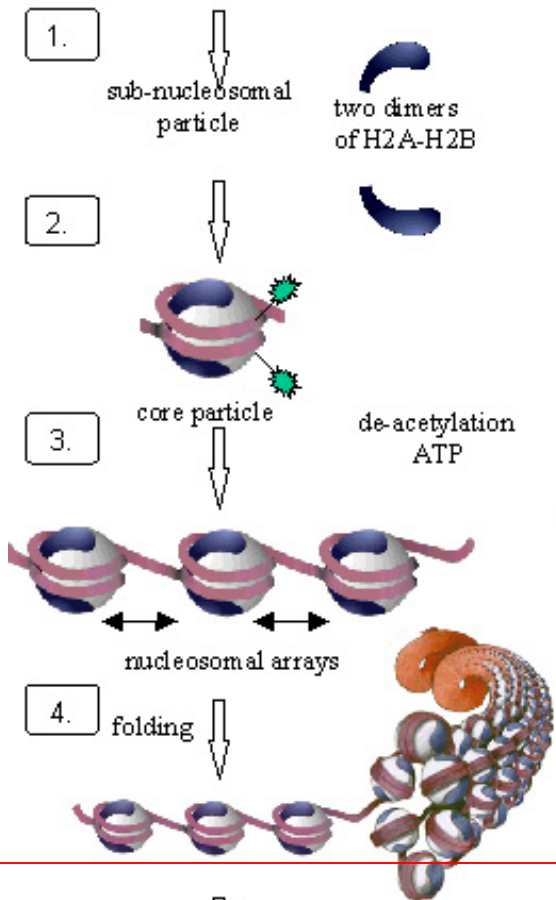




# Chromosome

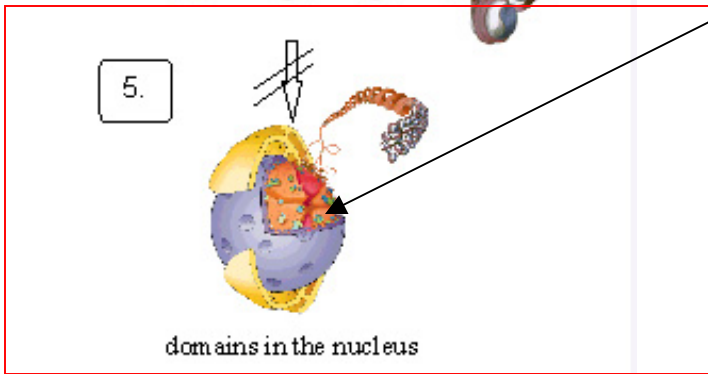
## Condensation Transition

DNA/Histone electrostatic attraction versus Bending Stiffness.



Known structures

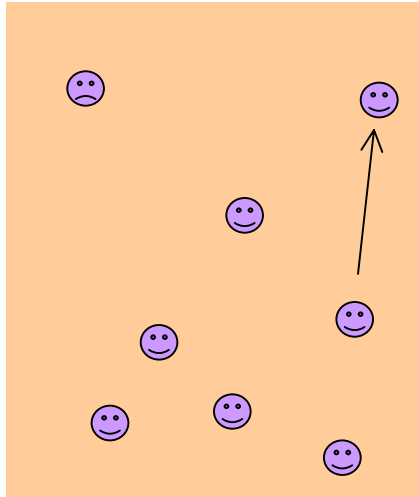
Nucleus: 23 chromosomes



Characteristic length  
for ionic dissociation/association in water:

The Bjerrum length  $l_B$

$$kT = \frac{e^2}{4\pi\epsilon\epsilon_0 l_B}$$



if  $d < l_B$  then  
ion pairing occurs

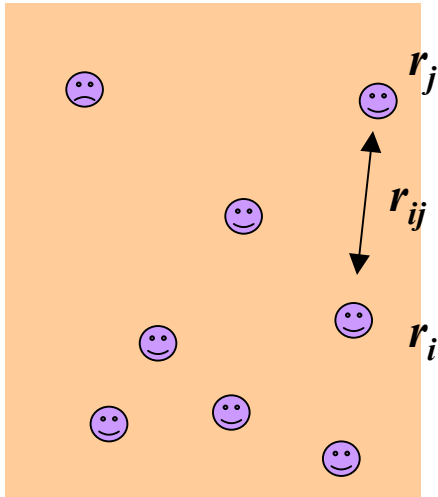
**In water,**  
 $l_B = 7.14 \text{ \AA}$

For a multivalent salt

$$z_i : z_j$$

*Association energy*  
*increases by  $|z_i z_j|$  and*  
 $l_B \uparrow$

# Simple salts



Potential at the arbitrary point  $r$  :

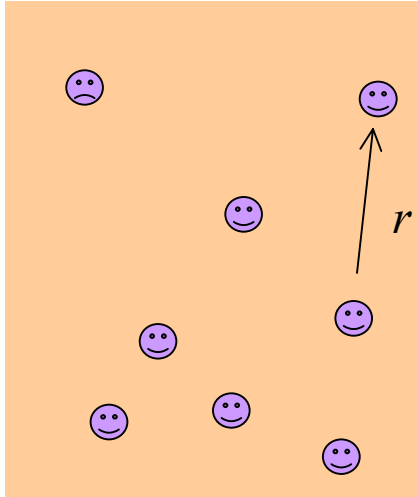
$$\psi(r) = \int \rho(r') dr' / 4\pi\epsilon\epsilon_0 |r-r'|$$

with  $\rho(r)$  the total charge density at  $r$

How does the charges distribution  $\rho(r)$  change with respect to the distance  $r$  from a central ion ?

$\rho(r)$  is related to  $\psi(r)$  by the **Poisson's** eq.,

$$\Delta\psi(r) = -\rho(r)/\epsilon\epsilon_0$$



If short range correlations are ignored (as in point ions),  
One can use the **Boltzmann's** distribution,

$$\rho(r) = z_+ e C_+^0 e^{-z_+ e \psi(r)/kT} + z_- e C_-^0 e^{-z_- e \psi(r)/kT} ,$$

The Poisson-Boltzmann (PB) equation.

Expanding exponential gives linearized PB or **Debye-Hückel (DH)** theory:

$$\Delta\psi = \begin{cases} 0 & \text{if } r < a \\ \kappa^2 \psi & \text{if } r > a \end{cases} \quad \kappa^2 = \frac{4\pi l_B \rho^*}{a^3} = \frac{4\pi \rho^*}{a^2 T^*}$$

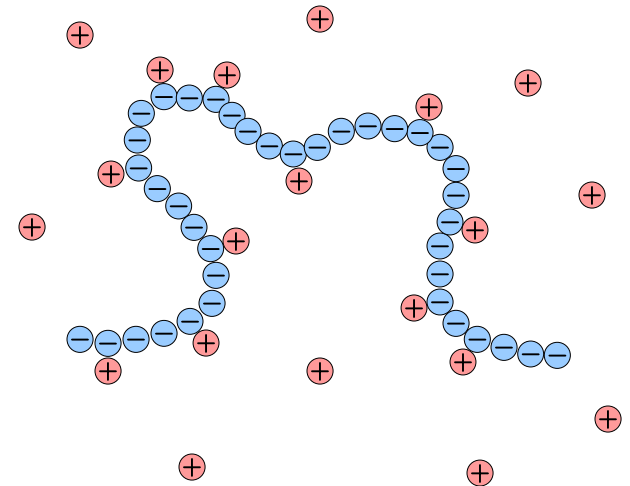
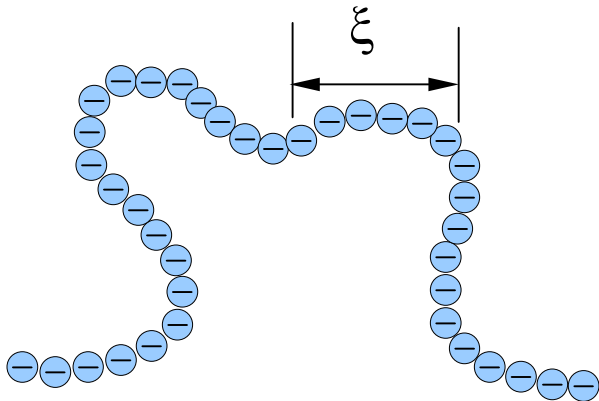
$$T^* = a/l_B$$

# Salt-free polyelectrolyte solutions, monovalent counterions

**In polyelectrolytes the linearized theories are not valid.  
The chains are strongly perturbed by electrostatics**

$$\xi \sim 1/\kappa^2 \approx (\rho^*)^{-1}$$

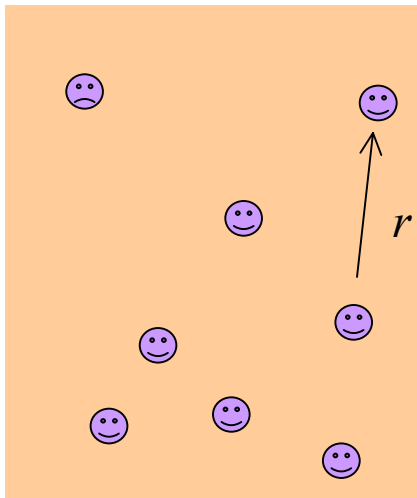
**They are stretched due to the repulsions**



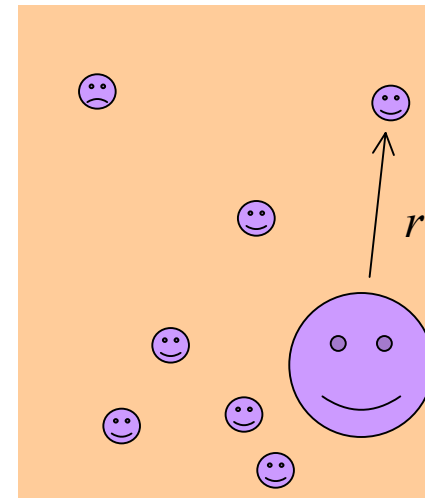
**BUT ion association along the chains: Shape depends on how many ions are around the chains**

# Non-linear effects in polyelectrolytes

Simple salt



Polyelectrolyte  
in ionic solution

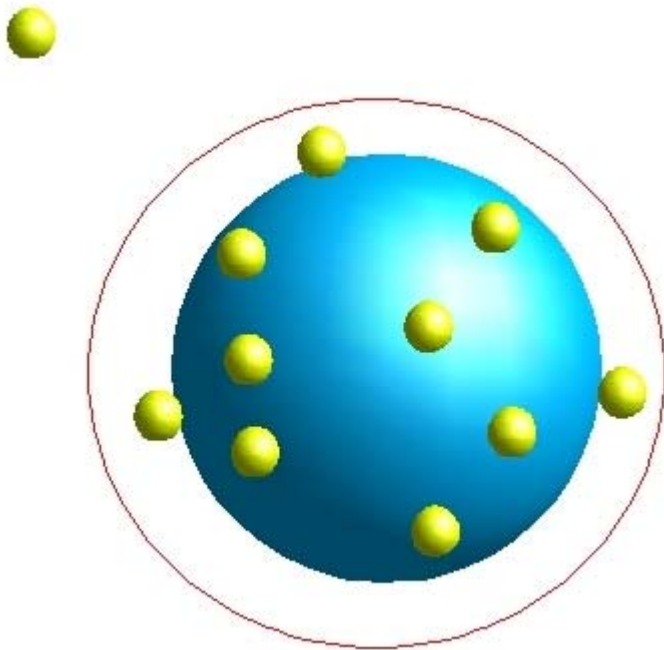


Apply  
similar  
calculation ?

- Start from the Poisson-Boltzmann equation
- BUT linearization is not possible because the approximation  $z_i e \psi(r) \ll kT$  is not valid → **ion pairing or ion condensation even at high  $T^*$**

In colloids the "condensed" ions renormalized the charge like a double layer in charged surfaces.

Away from the macroion the interaction with other charges reflects only the effective charge of the macroion, and follows mean field values (Debye-Huckel, DVLO).



**Warning.** Poisson Boltzmann ignores short range correlations, which can be important in the **dense** ionic region or **double layer**.

Infinite rods the charge density in Bjerrum length  $l_B$  units is

Monomers

$$z_m = -1$$

$$\xi_M = l_B / b \text{ the Manning parameter}$$

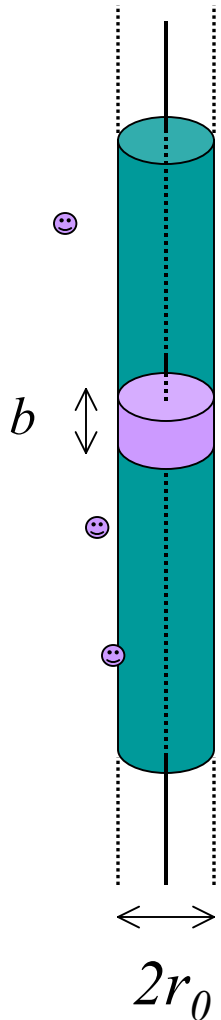
For B – DNA,  $b = 1.7 \text{ \AA}$  :  $\xi_M = 4.2$   
if  $> 1/z_c$  ion condensation

Counterions

$$z_c = +1$$

« free » ions treated in the Debye-Hückel approximation.

« condensed » ions reducing the monomer charge to an effective charge  $q_{eff}$ .





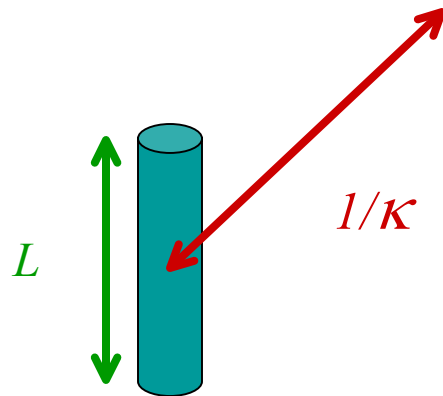
## Finite rods: the length effect

P. Gonzalez Mozuleos and M. Olvera de la Cruz, 1995

### Counterion charge renormalization in 3D, only at finite concentration

(Alexander et al., 1984)

Size and concentration effects



For charged spheres of size  $R$ , ion chemical potential far from the spheres, mainly entropic  $kT \ln C$ , on its surface, mainly enthalpic (electrostatic)

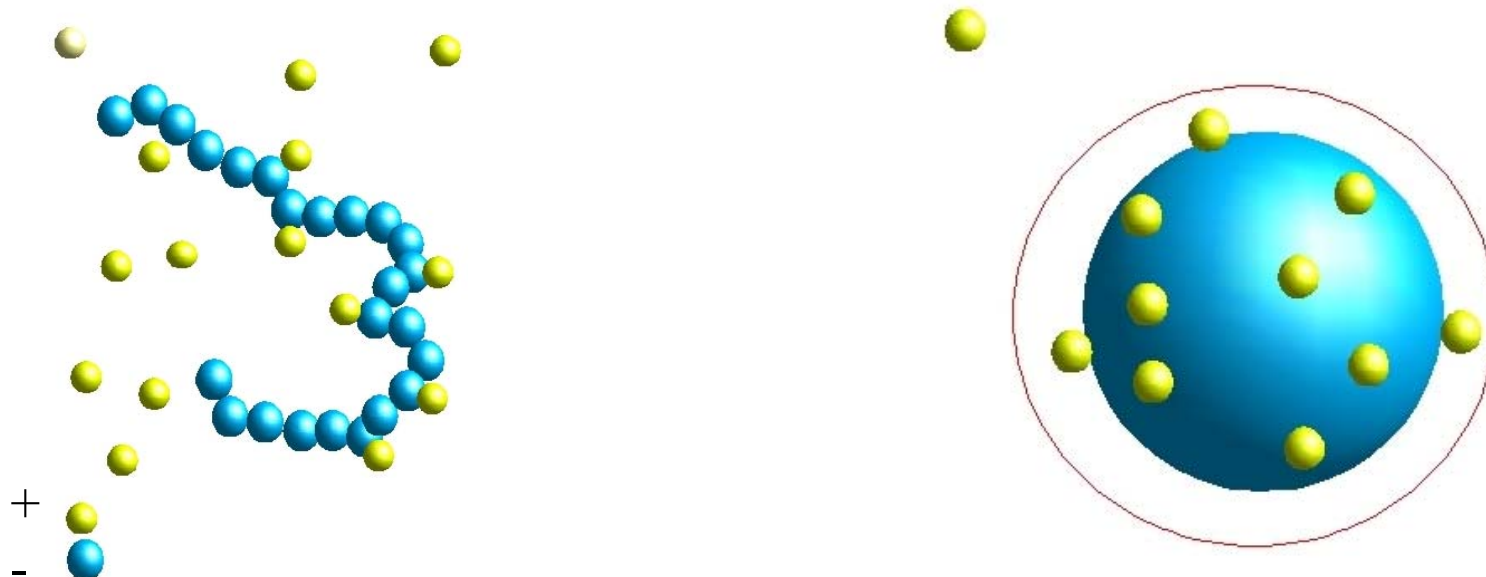
$$-q_{\text{eff}} e^2 / 4 \pi \epsilon \epsilon_0 R$$

$$q_{\text{eff}} \sim -R \ln C$$

The effective charge increases or the fraction of condensed ion decreases with dilution

For rods  $R \sim N$  and the chemical potential  $\ln N$  term

PB similar to equate chemical potential of free and condensed ions to determine the effective charge of the colloid. This can be done for any input charge distributions. For a fractal chains we input the distribution from the center of mass and allow the ions to “penetrate” the fractal.



+  
-

$$R \sim N^{\nu}$$

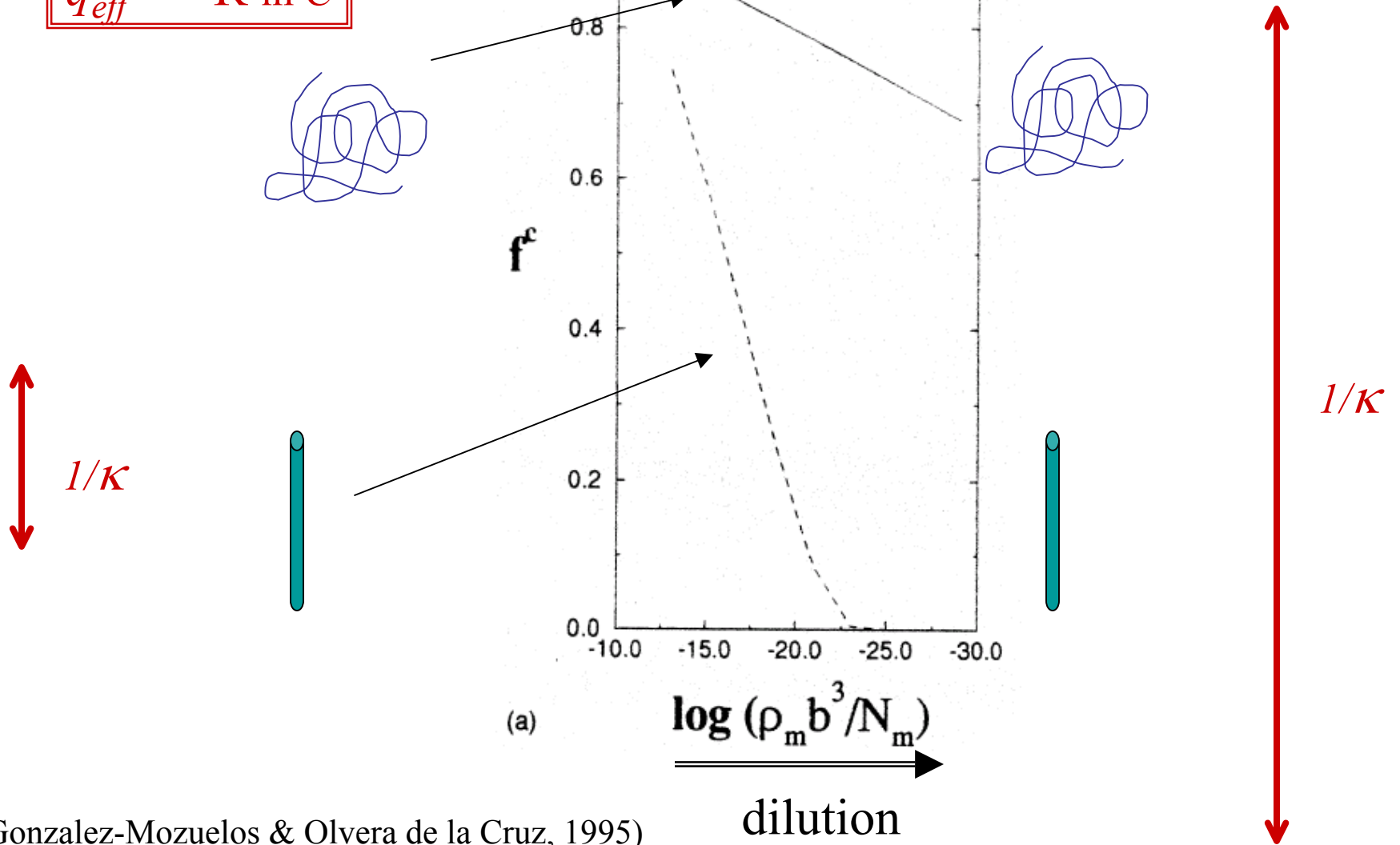
$\nu = 1$  rod

$\nu = 1/2$  random walk

$\nu = 1/3$  dense ionic  
structure

Conformation effects: fraction of condensed counterions (DH for ions only, no chain RPA contribution)

$$q_{eff} \sim -R \ln C$$



(Gonzalez-Mozuelos & Olvera de la Cruz, 1995)

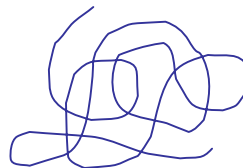
dilution

Poisson-Boltzmann gives rod lowest energy though **more ions are condensed in collapsed than in rod.**

**IF SHORT RANGE CORRELATIONS**  
as charge density increases or valence of counterions increases then collapse chains

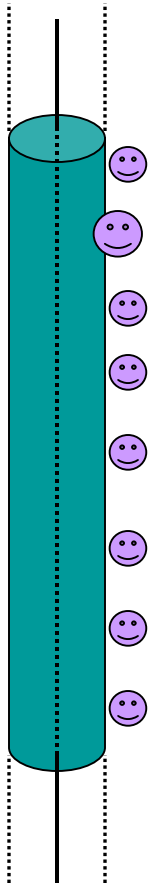
Collapse to denser system of charges due to counterion induced attractions

**Z=4.**

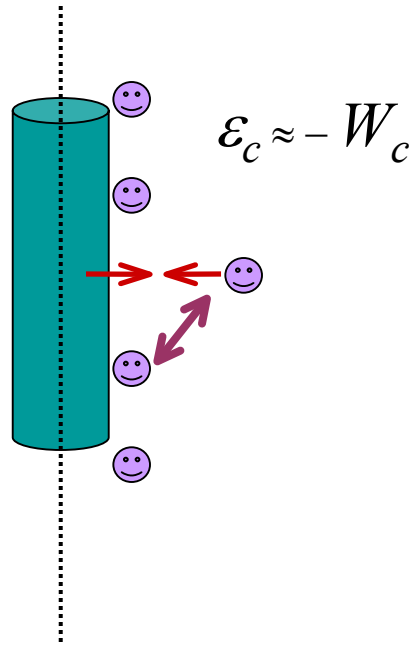


**Z=1.**

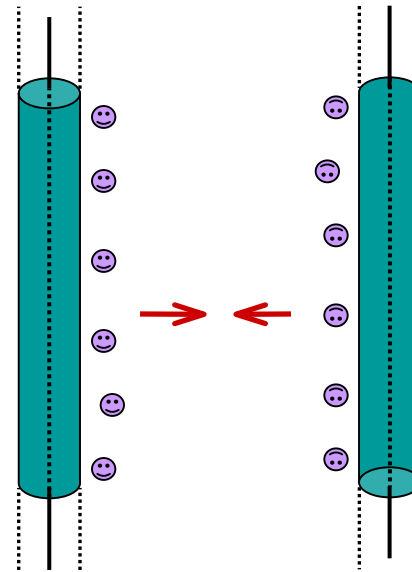
Two-dimensional lattice of the multivalent counterions around the surface (Rouzina and Bloomfield 1996) and around rods (Arenson et al 1999, Solis and Olvera de la Cruz, 1999)



Correlation energy  $\epsilon_c$   
per ion  $< 0$  (attractive)



If  $n$  : local concentration of  
the correlated liquid



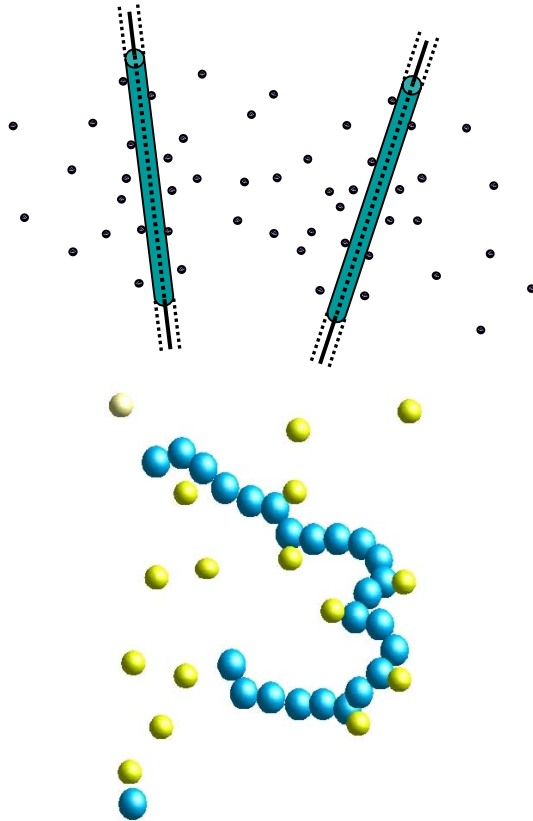
$$\epsilon_c(2n) < \epsilon_c(n)$$

Attraction between chains

# Phase separation of polyelectrolytes with the addition of multivalent ions

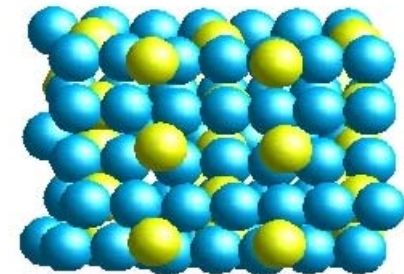
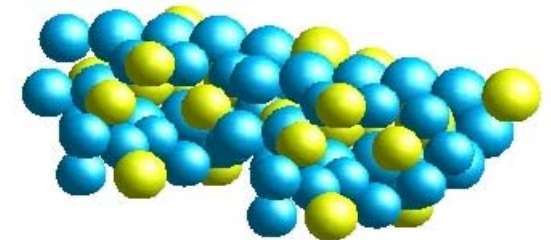
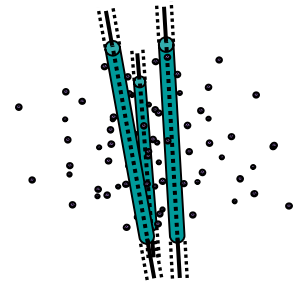
## In dense systems

Highly correlated ions leads to attractions (Modified D-H gives no transition in salt solutions)



$e^{-Kr}$  Repulsions only in dilute with point ions

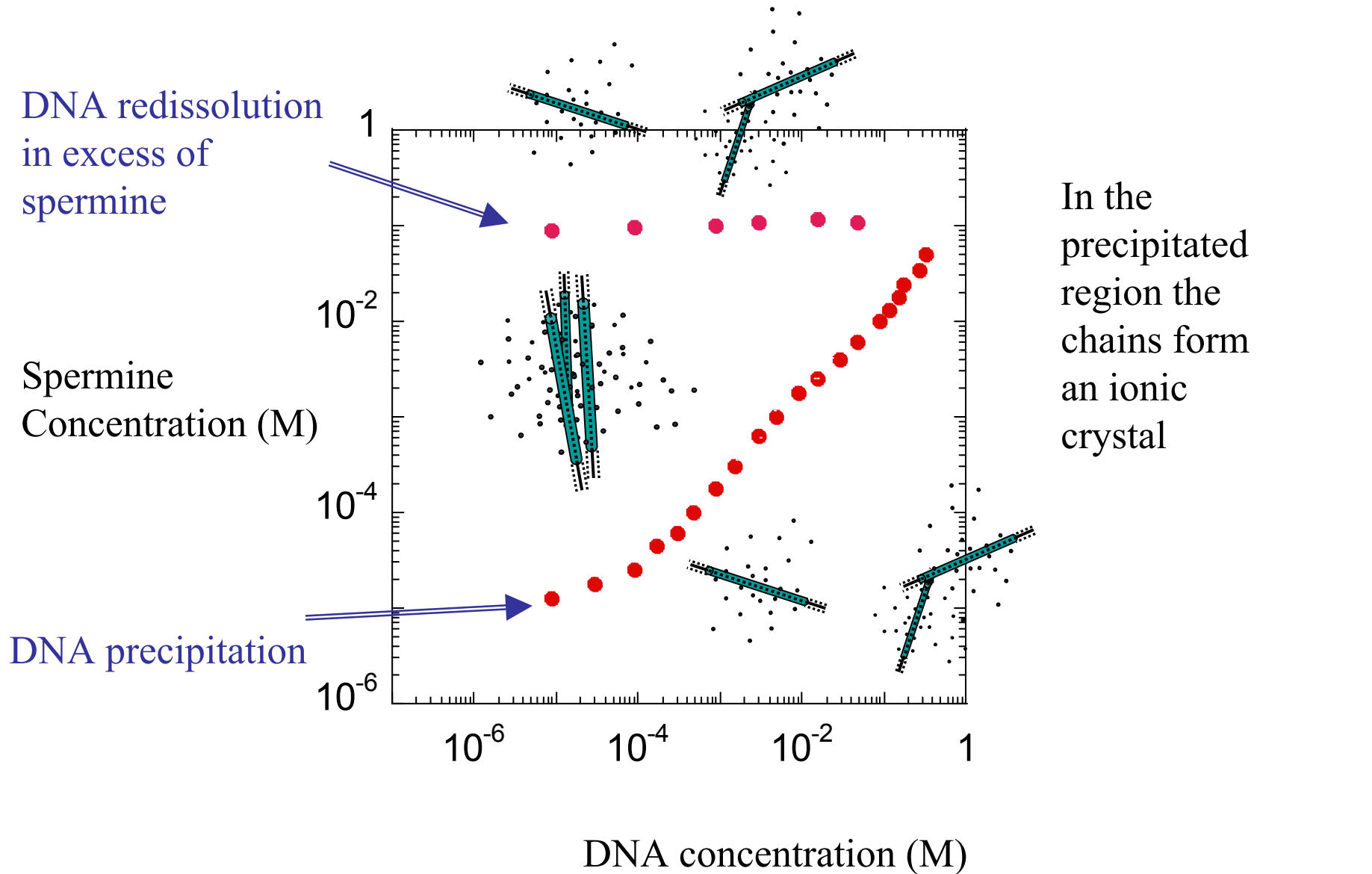
(Brenner & Parsegian, 1972)



Ionic glass

(Solis + M.O. de la Cruz, 2000, 2001)

# Phase diagram: nearly universal



(Raspud et al., 1998-99)

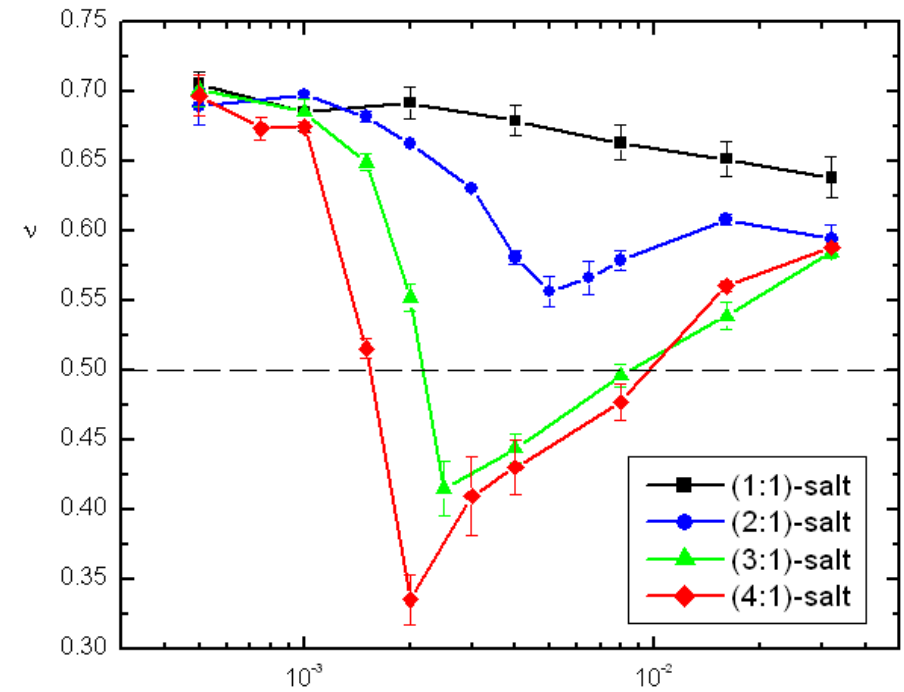
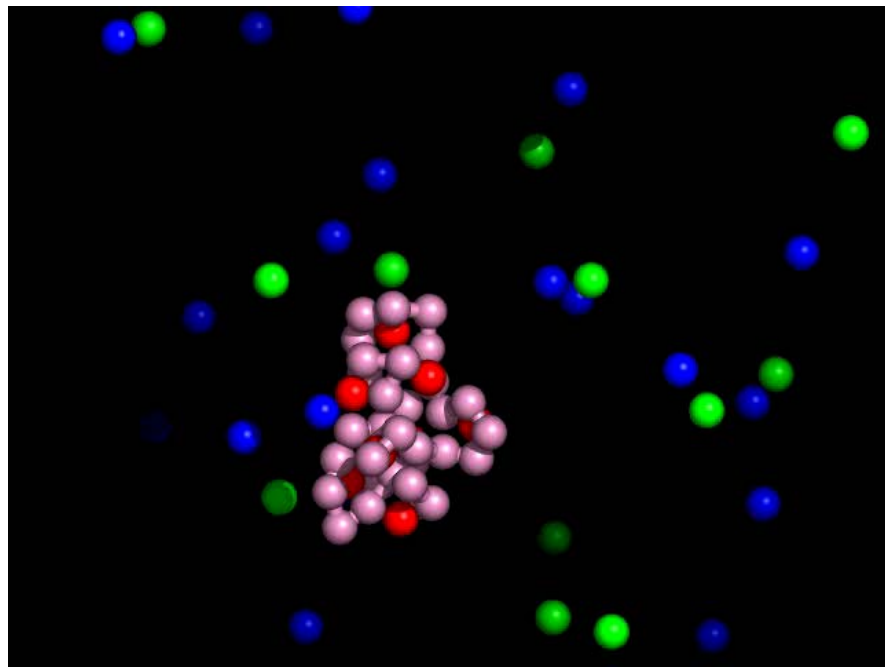
Polyelectrolyte (PE) Chains in multivalent ions (Gonzalez-Mozuelos et al 95; Solis et al 00, 01; Lee + Thirumalia 00; Liu + Muthukumar 02))





**E. Luijten 04**

$$\sigma_m \approx 2.5 \text{ \AA}; \text{ water at 298K: } l_B \approx 7.1 \text{ \AA} \Rightarrow l_B / \sigma_m \approx 3; C_m = 0.008 \sigma_m^{-3} \sim 1 \text{ M}$$

**PE(N=32) + 8(4:1)salt**

**Scaling description:  $R_g \sim N^\nu$**

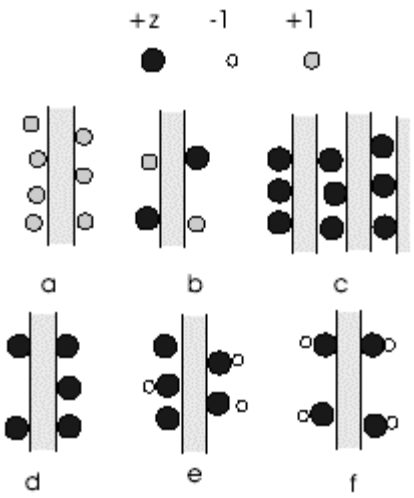


-  mer Charged rods (DD DNA) the precipitation is into bundles
-  (+1)
-  (+4)
-  coion

- $\nu = 1/3$  sphere
- $\nu = 0.5$  ideal chain
- $\nu = 0.588$  coil
- $\nu = 1$  rigid rod



# Effective charge

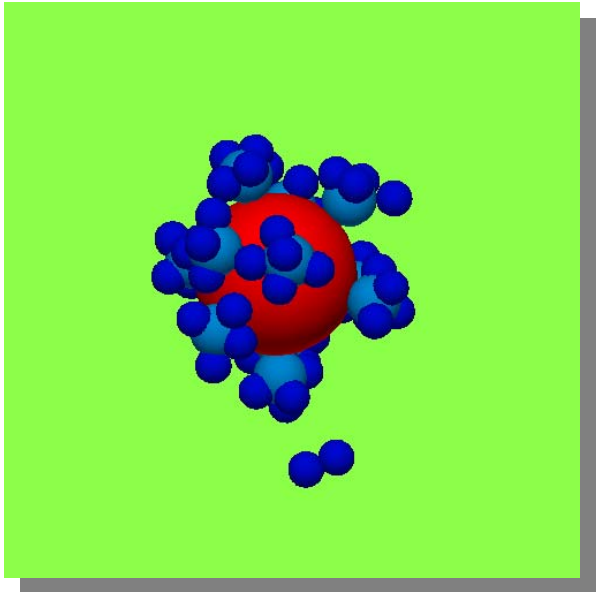


d=positive; e=Neutral, f=negative

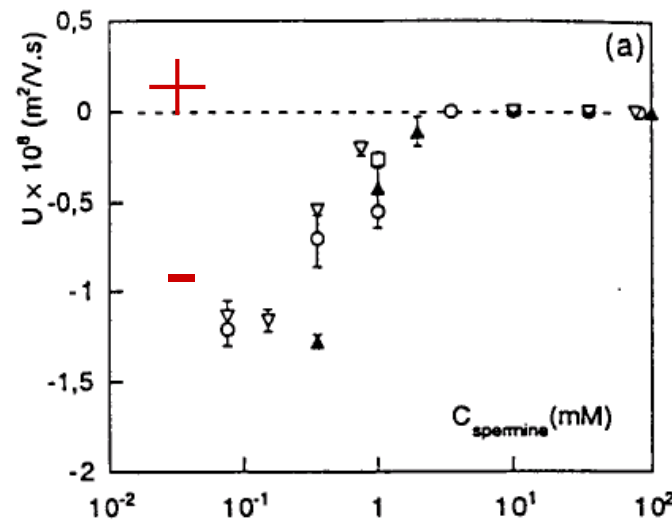
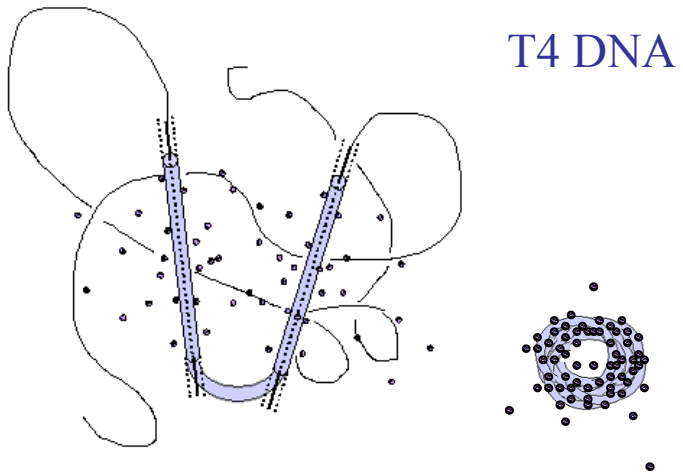
**Polyelectrolytes collapse; beyond neutralization, re-expansion occurs because the multivalent ions can interact more with co-ions**  
**Counterion size has crucial role.**

Solis + MO de la Cruz 00, 01;  
 Mesina, Holm and Kremer 00; Solis 02, Grosberg et al 02, Grosberg + Tanaka 01

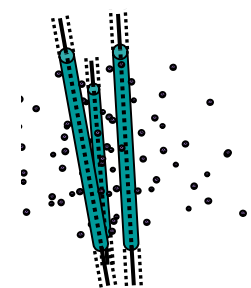
**Stability of complexes to segregation or to dissolution**



# Experiments on charge inversion,

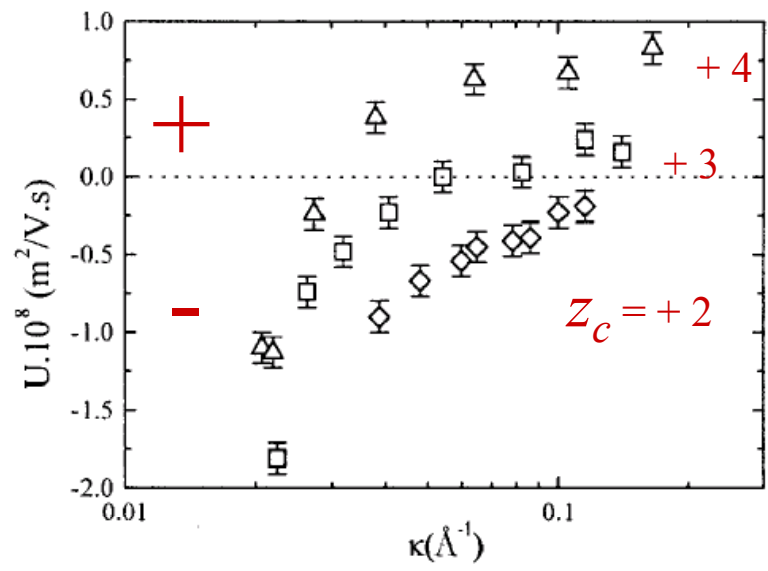


Short DNA fragments

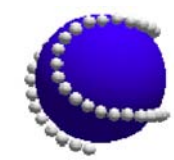


Spermine concentration ( $Z_c = +4$ )

## Linear DNA



Nucleosome Core Particles

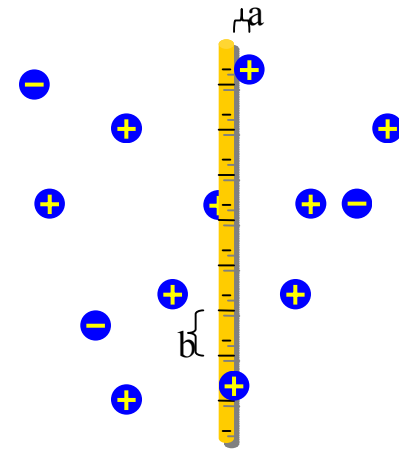
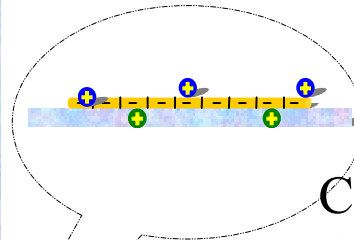
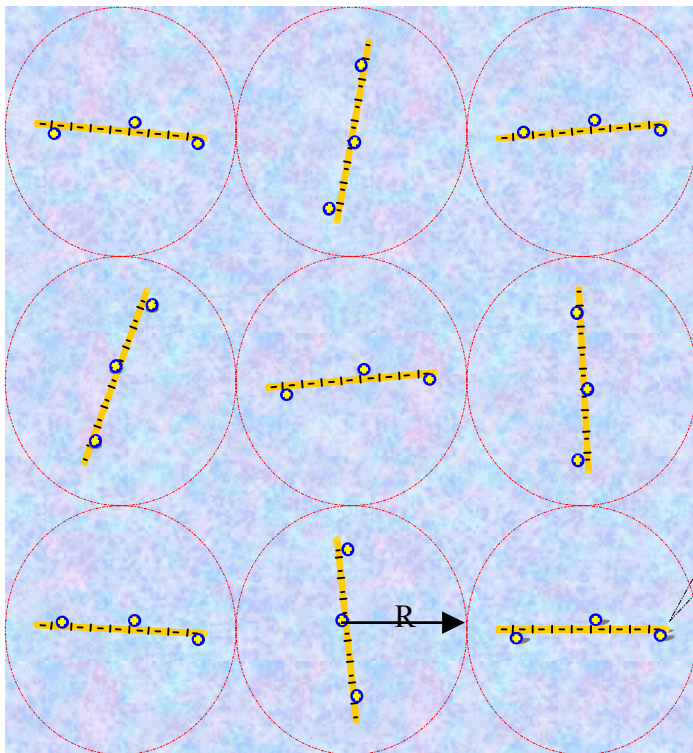


Spermidine concentration ( $Z_c = +3$ )

No charge inversion

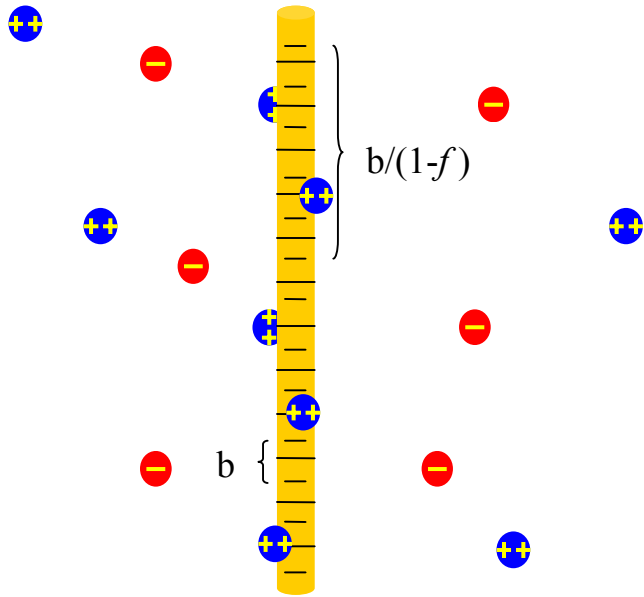
# Adsorption of Strongly Charged Polyelectrolytes onto Oppositely Charged Surface

Driving force: counterion release

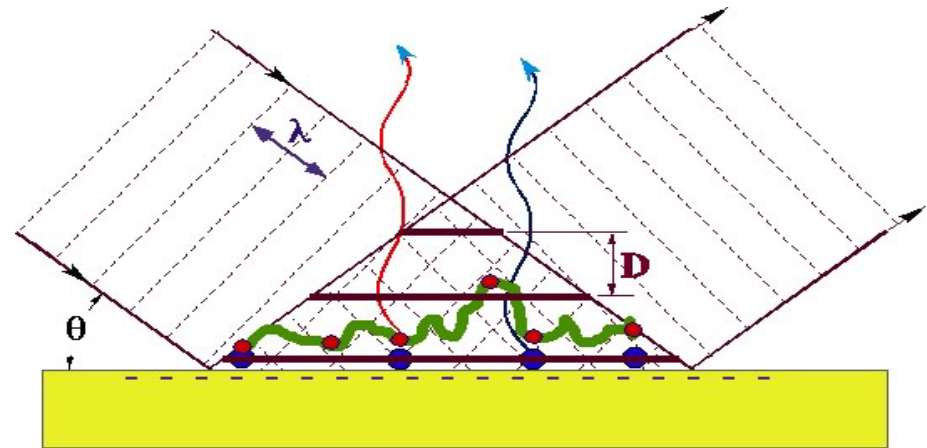


Correlations along surface if distance between rods larger than adsorbed layer thickness (break down of PB) leads to charge inversion (Netz+ Joanny 99; Dobrynin+ Rubinstein 00).

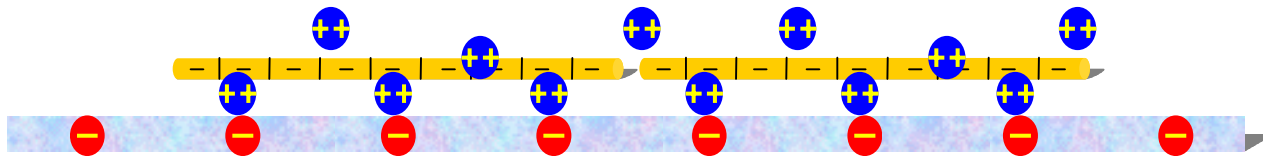
# Strongly charged rods in divalent solution

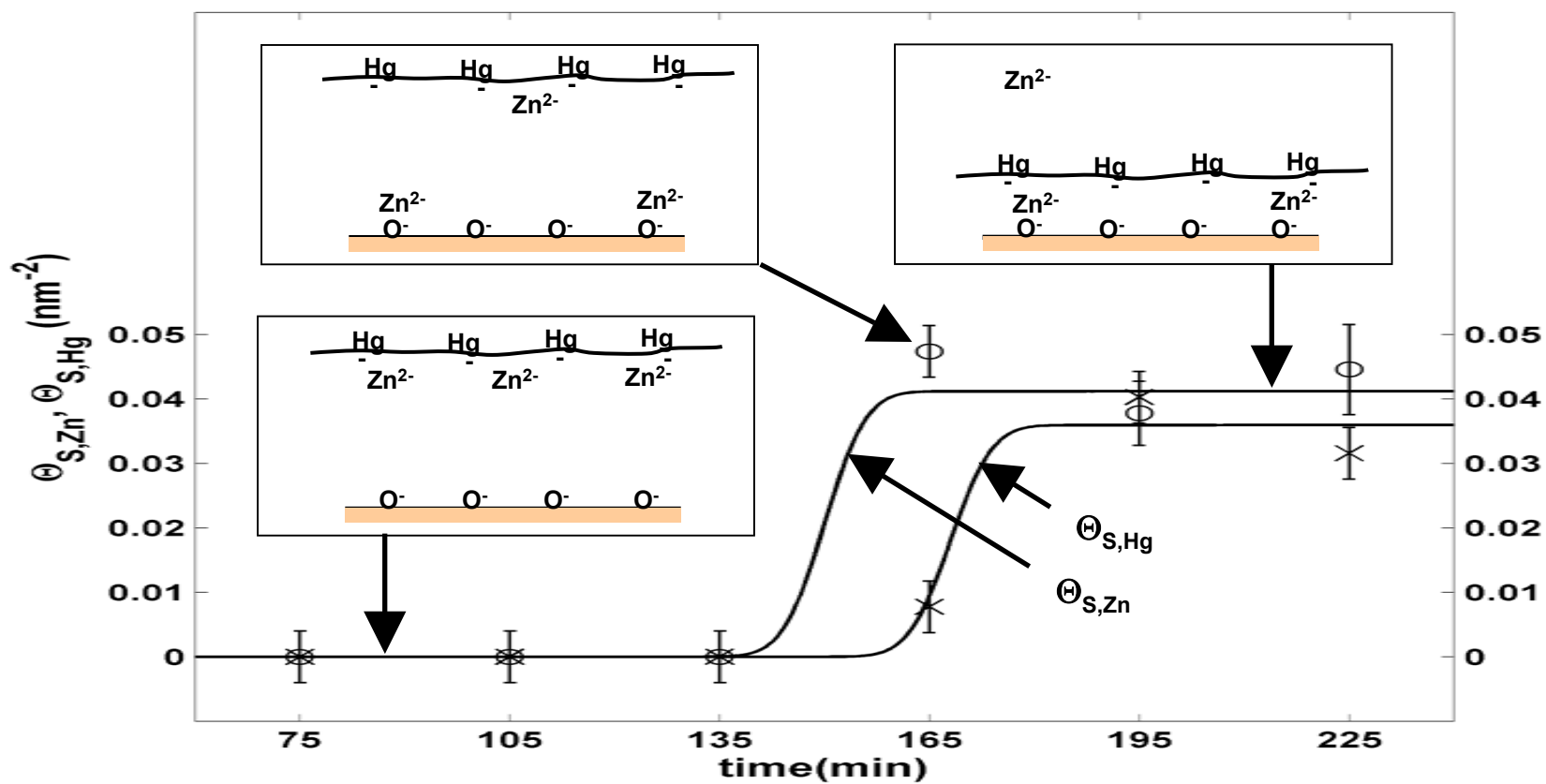


Polyelectlectrolytes adsorption onto same charged surfaces studied experimentally via X-Ray Standing waves (Libera, Cheng, Bedzyk).



Adsorbed rods via short range attractions





Time dependence of the Zn and Hg surface condensed layer coverages. The line is drawn to guide the eye.

# Conclusions on precipitation

**We have proposed a mechanism for attractions of purely electrostatic nature that describes the phase diagram.**

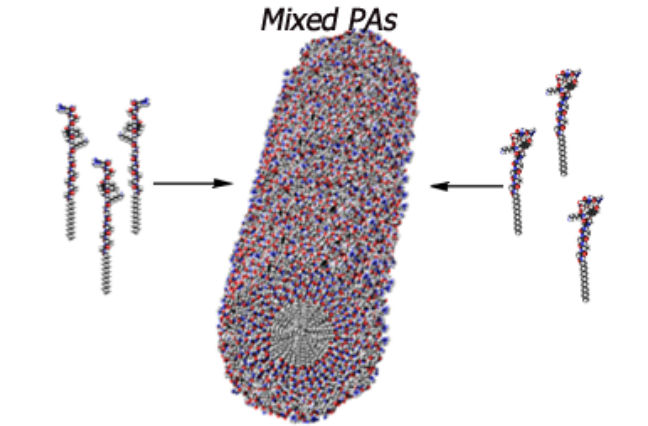
**Smaller multivalent ions are more efficient condensing polyelectrolytes. In order to observe re-dissolution by adding more multivalent ions one needs small association constants.**

Mixture of mono and  $z_c$ -valent cations condensed onto the DNA induce non-universal phase diagrams

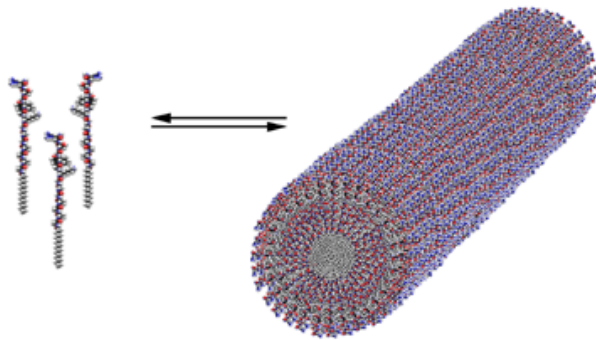
The non-ideal behavior of the “free” multivalent salt (determine by effective ionic sizes) reduced and may suppressed the DNA overcharging

Surface adsorption of polyions described by correlations.

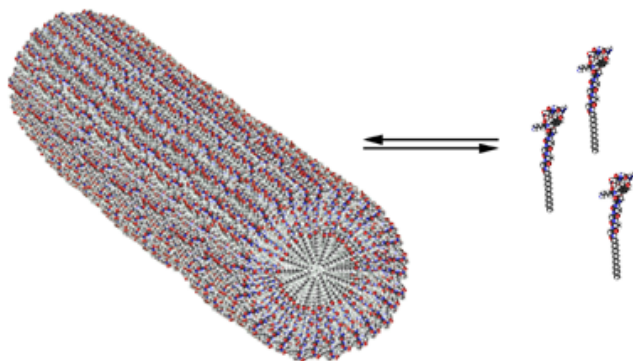
Equal charge surface adsorption is possible via oppositely charged ions of valence  $2+$  (like – cell membranes to – DNA)



Basic PA



Acidic PA



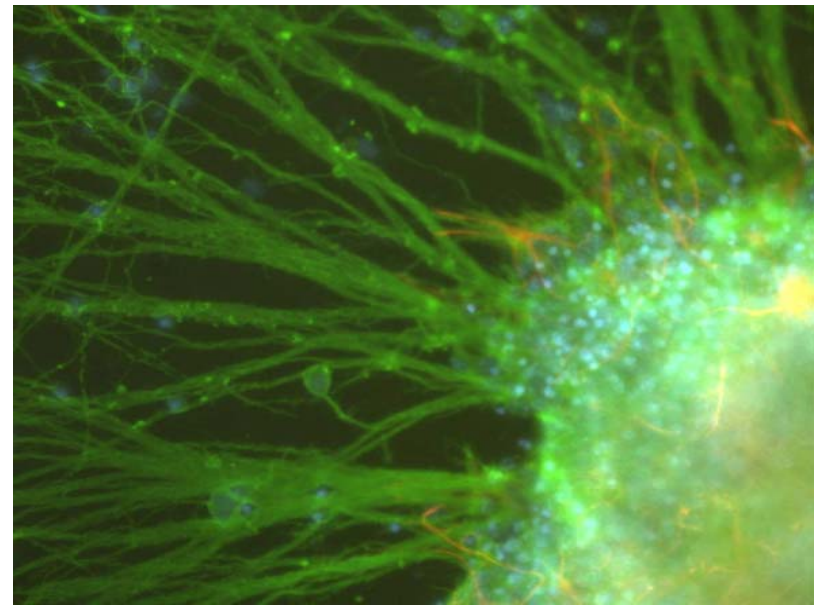
pH<4

pH>9

**Peptide Amphiphiles (PA) nanofibers formed from acidic PAs by dropping the pH below 4.5 (low). Basic PAs self-assembled above pH 9 (middle).**

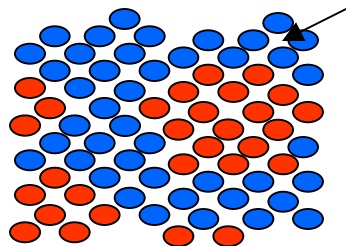
**Combining acidic and basic PAs at neutral pH self-assembly (top).**

**Only form cylinders. (S. Stupp lab for use as cell support such as laminin)**

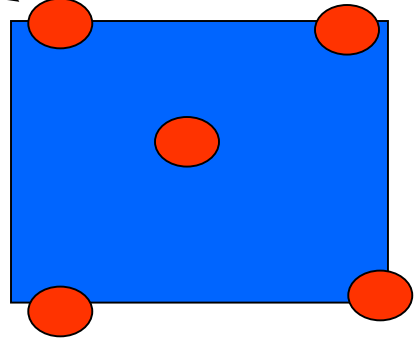
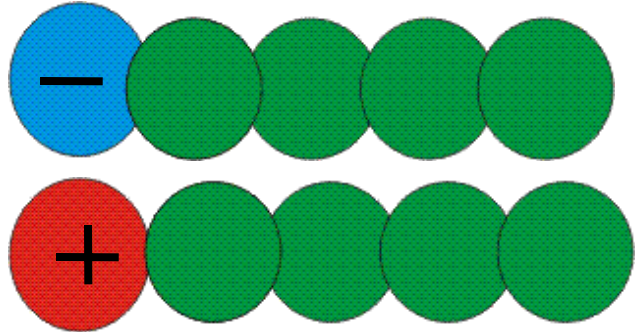


# Multi-component micelles? (Solis, de la Cruz, Stupp 04)

Use oppositely charge units to built stable nano-aggregates with surface structure if units are otherwise immiscible.



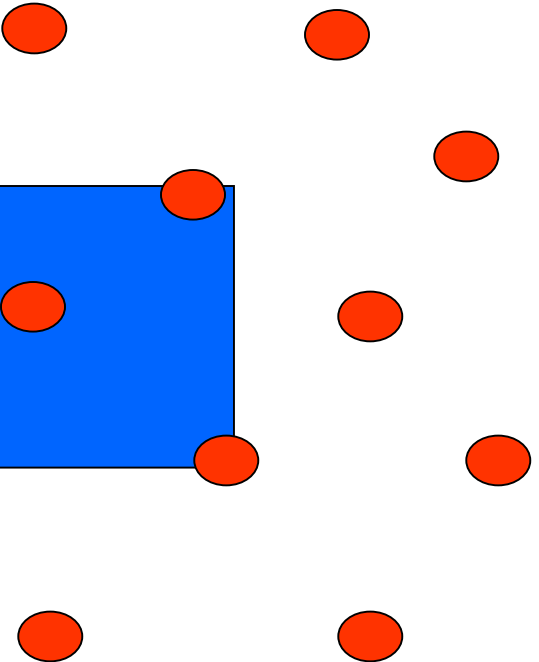
$\gamma_0$



Flat surface pattern due to the competition of surface tension  $\gamma_0$  and charge density  $\diamond$ :

domain of size  $L \sim A^{1/2}$  is  $L \sim (\gamma_0 / \diamond^2)^{1/2}$

The fraction of area  $f$  of one unit in the cell of area  $A$  determines the pattern structure.

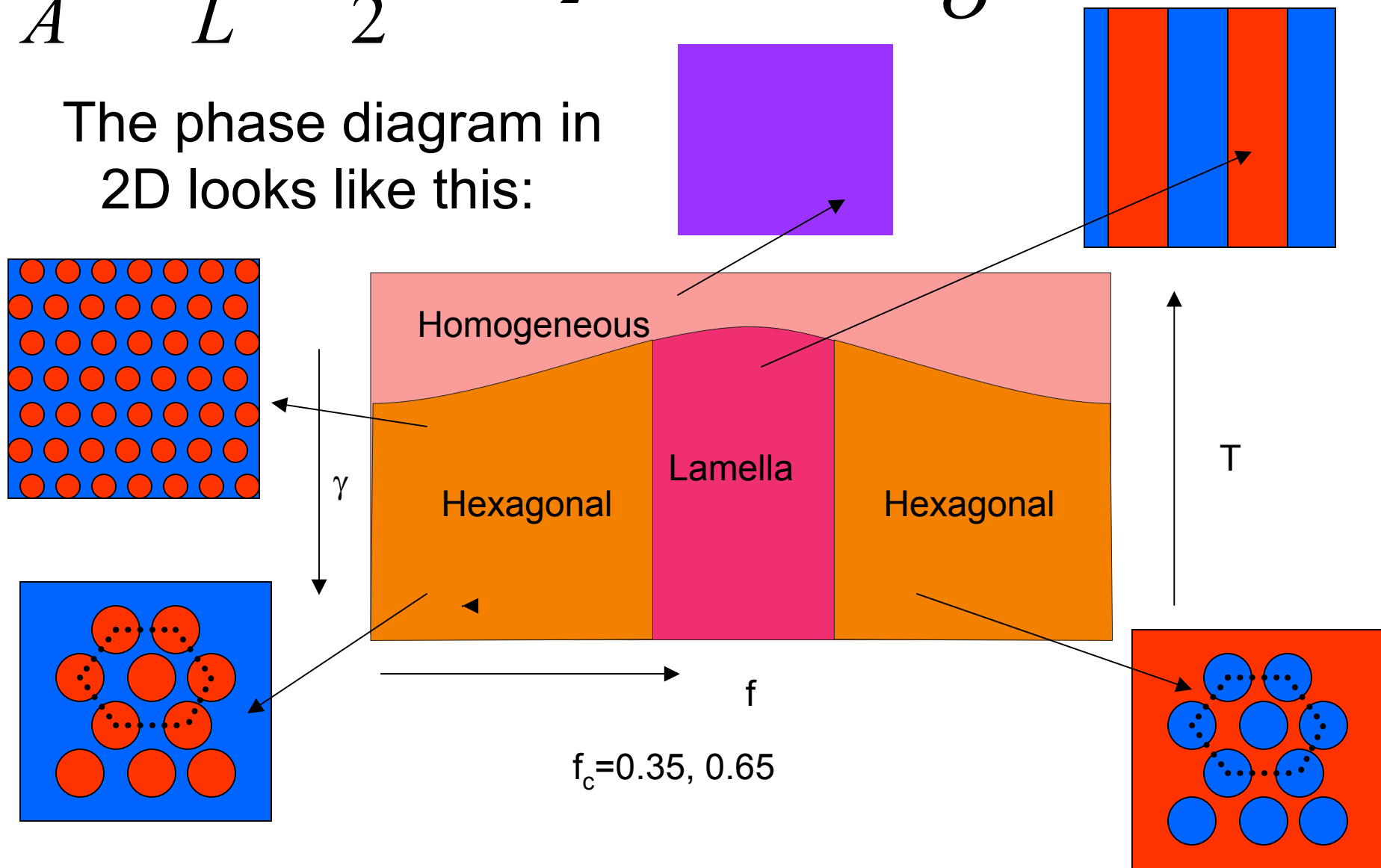


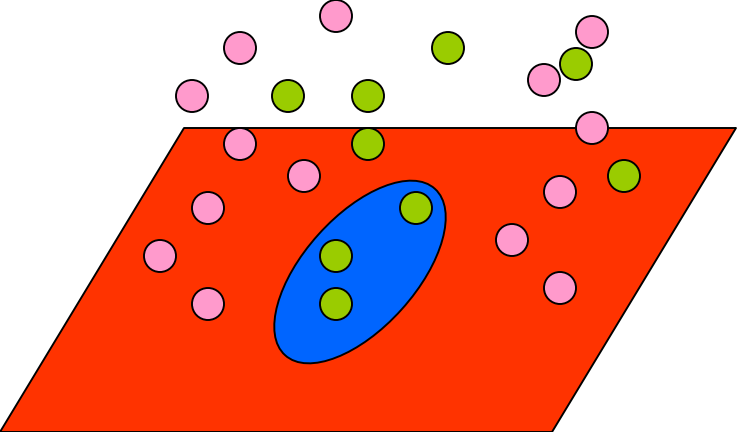


$$\frac{F}{A} = \frac{\gamma s_1}{L} + \frac{1}{2} \sigma^2 L s_2$$

$$A_o = \frac{\gamma}{\sigma^2}$$

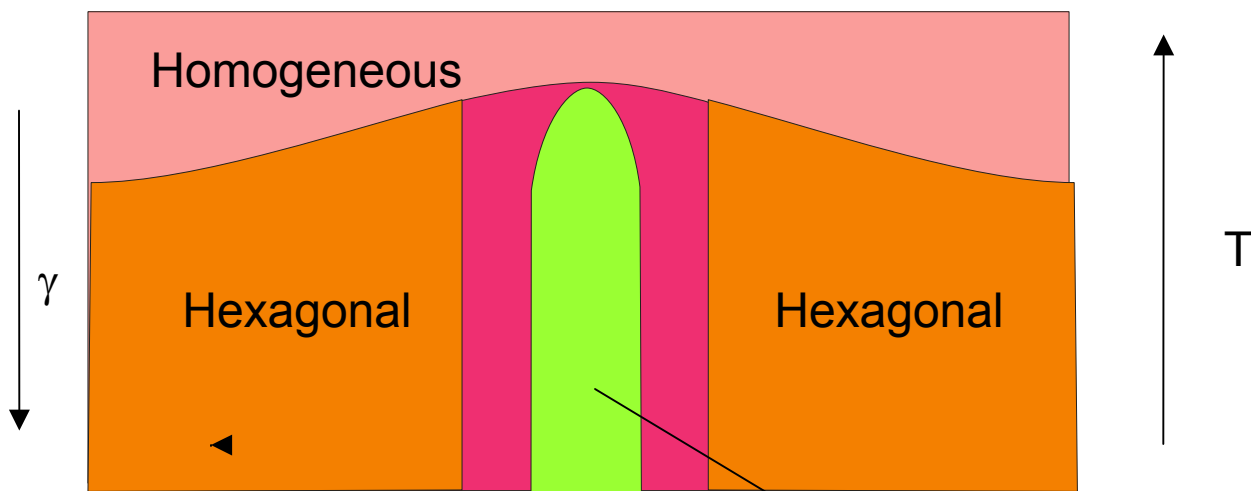
The phase diagram in 2D looks like this:



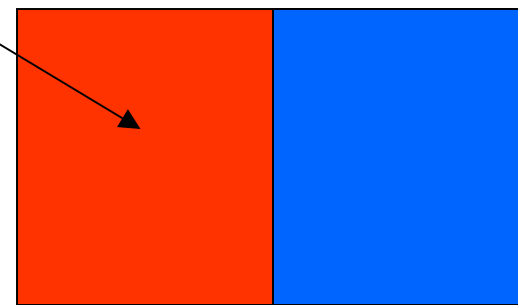


Pure Coulomb  $F \sim L$   
 Screened  $F \sim L, L < 1/\xi$  or  $F \sim 1/\xi, L > 1/\xi$

Macrophase segregation

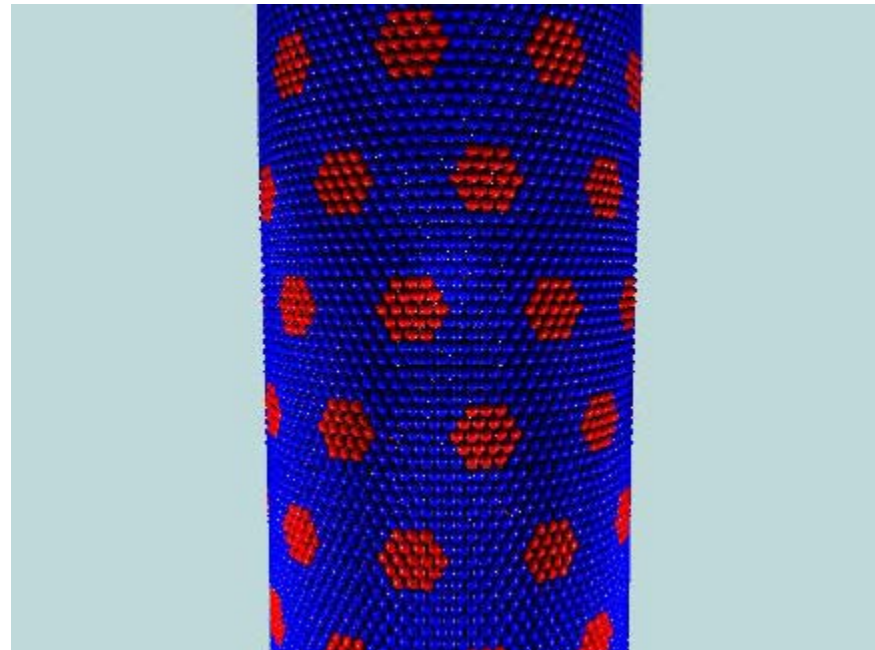
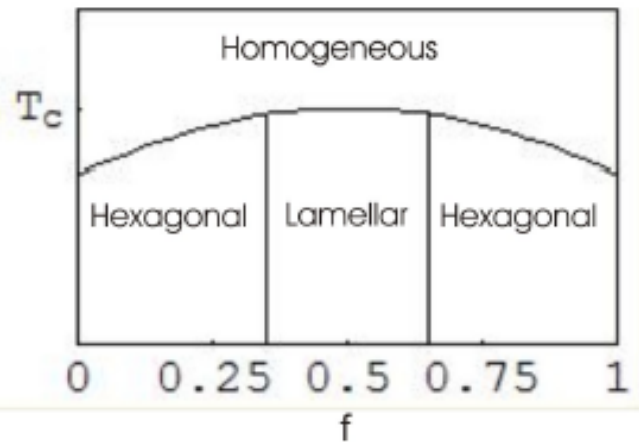


Full segregation



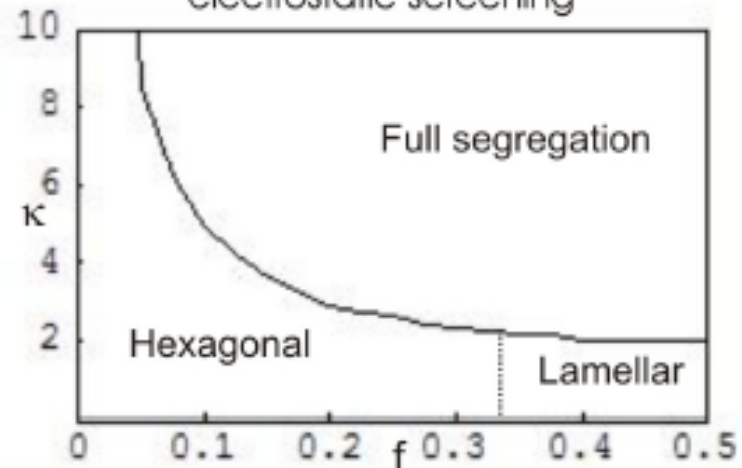
# Electrostatics generate multicomponent micelles and vesicles with surface patterns

Phase diagram for a flat geometry



**With screening the domain size jumps from finite to macroscopic segregation**

Phase boundaries in the presence of electrostatic screening

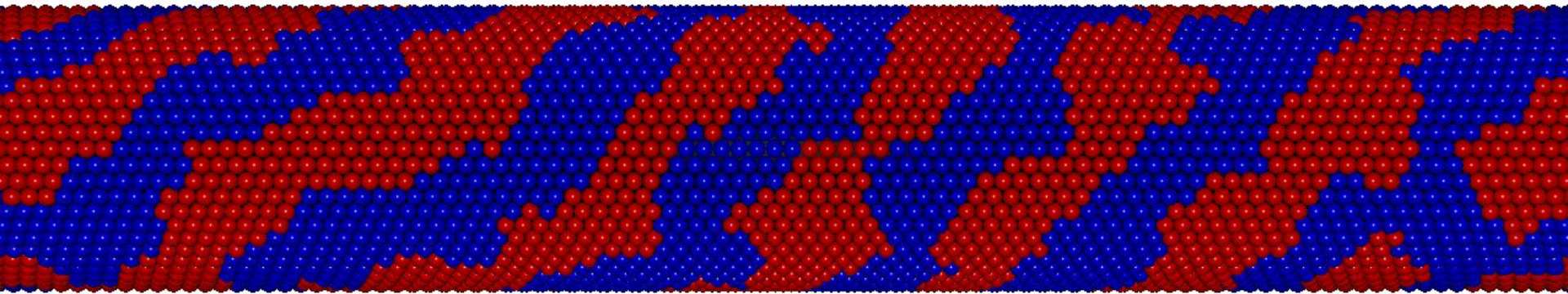


## MONTE CARLO EQUAL SIZE AND OPPOSITE CHARGE

+1 and -1

Sort range =  $3KT$  ,

Electrostatic  $1/\epsilon \sim .1$



Conclusion: in two dimensions one can create periodic patterns using the competition among electrostatic and van der Waals interactions